

the authors are of the same material, it would be meaningful to estimate the life of the whole assembly.

Authors' Closure

The authors wish to thank Dr. Liu for his discussion. The discussor suggests that the agreement between deflections of the cantilever plate predicted by the finite element method be compared to the results of the explicit solution. We agree that whenever it is possible to make such comparisons that they be made. However, the example considered was chosen in order to demonstrate the technique of analysis rather than solve a particular problem and for this reason comparisons with Jaramillo's results were not made. In practice, where more complex cross sections are normally encountered, explicit form results are often precluded. In these instances characteristics of the load distribution can be found with relative ease by employing the methods indicated herein.

With regard to the question of assembly life estimate, life prediction for the assembly is an important design consideration and can be determined by computing individual component lives and combining these as demonstrated in equation (17).

First Effects of Stokes Roughness on Hydrodynamic Lubrication¹

K. Tonder.² The authors are to be congratulated for having attacked a very important problem in lubrication. Their work is an impressive piece of mathematics and puts a question-mark to some of the basic assumptions implicit in Reynolds' equation.

However, such a question-mark must also, according to this discussor, be put on their results. The latter are closely tied up with expressions (37). These are in fact the decisive factor in the deviation from previous roughness theories, allowing an infinite increase in the load capacity.

The authors are aware of this since they write, "Expressions (37) might leave the impression that the roughness effects could become unbounded if β or λ were chosen arbitrarily small. But these parameters are closely tied with the roughness spacing. If the roughness spacing is smaller than the film thickness, the RHS of equations (2) and (3) are dominant and then the iterative method fails. In fact, our results should be increasingly better when the RHS of equations (2) and (3) are increasingly small."

Certainly these parameters are tied up with the roughness spacing, and so the approach would fail for a very dense roughness pattern. But basically the applicability of the results cannot be assessed from

¹ By Dah-chen Sun and Kuo-Kuang Chen, published in the January, 1977, issue of the JOURNAL OF LUBRICATION TECHNOLOGY, TRANS. ASME, Series F, Vol. 98, pp. 2-9.

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the physics of the problem because it is the mathematical form of (37) that is important. Which parameter values are permissible?

This discussor finds it very unlikely that the inclusion of the Stokes terms in (2) and (3) would produce an infinite load capacity, even theoretically, when the roughness spacing tends to zero. Therefore, since formally expressions (37) may become unbounded, an additional correction must also have the possibility of tending to infinity with decreasing roughness spacing, in order to cancel the unboundedness. But then this term should also be included in the solution.

This has to do with the possibility that the iterative process may be nonconvergent. This has not been considered by the authors. What is the reason for this?

Alternatively, assume that the process is (rapidly) convergent with a proper initial iterant.

In order that the load expression of (31) may be bounded, its two last bracketed terms (or their "correct" equivalents) must be of the order of β^2 , λ^2 and β^4 , λ^4 , respectively. This means that one is facing a case of subtraction of terms consisting of components of very different orders of magnitude.

As is well known this may cause serious errors if the terms involved are not extremely accurate. Though the pressure profile expressed by (7) may not deviate much from the correct one satisfying (1)-(3), it may be quite inadequate as an initial iterant because of the high derivatives appearing in the expressions—which may deviate widely from the true value—and, possibly, also because of its combination with the velocity expressions of (7).

The discussor has not been able to find any formal error in the analysis, and though he has doubts about the correctness of the direct results, he feels that in many ways the approach is interesting and should be pursued further.

The discussor would appreciate the authors' comments on the above suggestions.

Authors' Closure

The authors commend Professor Tonder for the reiteration of the validity and limitations of their results. The main contribution of the paper was represented by equations (31) and (32), while in equation (36) a general form of the autocorrelation function (ACF) of roughness height was postulated. As stated in the paper and also pointed out by Professor Tonder, the two parameters β and λ used to characterize the ACF relate directly to roughness spacing. They are of the same order of magnitude of ϵ and can not be infinitesimal.

The use of the Stokes equations inherently assumes that continuum mechanics applies and inertia terms are negligible. It is the iteration scheme used in the paper to solve the Stokes equations which imposes a limitation on the smallness of β and λ . Thus we are not considering the case of roughness frequency approaching infinity. The parameters β and λ dictate the rate of convergence of the iteration solution. For large β and λ , the Stokes terms of the solution diminish and the Reynolds solution is resulted. The iteration solution is not valid for very small β and λ (compared to ϵ) as discussed in the paper. Professor Tonder is right that the problem of convergence of the iterative solution should be pursued further.